

Do Now: what is the square root of 9 ?

square root of 16 ?

square root of 36 ?

## Rational and Irrational Numbers:

Rational numbers terminate, can be written  
Ex: 3, 1.75,  $\frac{1}{5}$  as a fraction  $\frac{a}{b}$   $b \neq 0$

Irrational numbers do not terminate

Ex:  $\pi$ ,  $0.\bar{3}$ ,  $\sqrt{6}$

R or I?

Ex:

① 9.05 R

②  $0.\bar{3}$  I

③  $\pi$  ~~I~~

④  $\frac{1}{5}$  R

⑤  $14.35\bar{17}$  I

⑨  $\sqrt{64}$  R

⑥ 21.4375 R

⑩  $\sqrt{8}$  I

⑦  $84\frac{1}{2}$  R

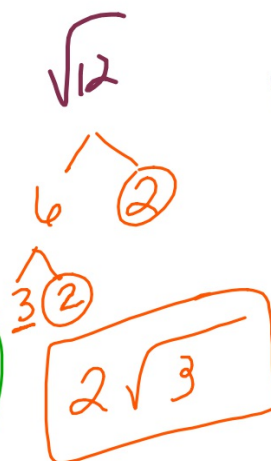
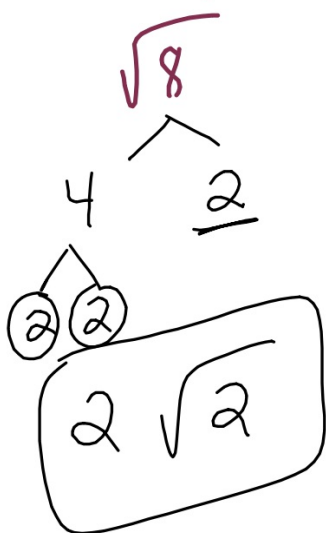
⑧  $\frac{1}{9}$  R

Radical number under square root symbol  $\sqrt{\quad}$

2 ways to simplify radicals:

- ① Factoring: exact answer (irrational #s)
- ② Area Model: approximate answers (rational #s)

# Factoring Radicals:



## Perfect Squares

$$1^2 = 1$$

$$2^2 = 4$$

$$3^2 = 9$$

$$4^2 = 16$$

$$5^2 = 25$$

$$6^2 = 36$$

$$7^2 = 49$$

$$8^2 = 64$$

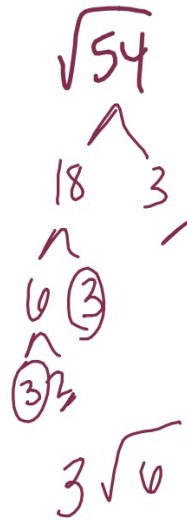
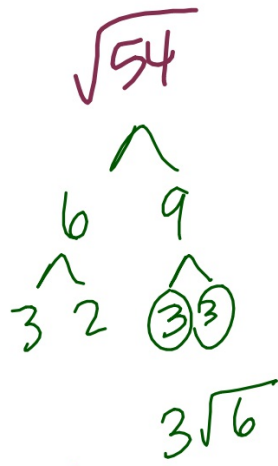
$$9^2 = 81$$

$$10^2 = 100$$

$$11^2 = 121$$

$$12^2 = 144$$

Factoring:



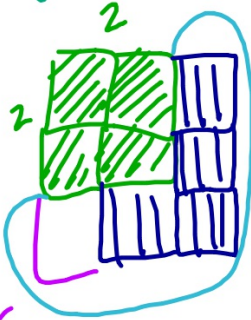
HW:

Factor to give exact answer:

- ①  $\sqrt{27}$
- ②  $\sqrt{32}$
- ③  $\sqrt{192}$

# Simplifying by Area Models:

$$\sqrt{8}$$

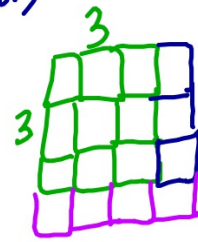


added  
to make  
a perfect  
square

← add 4 (numerator)  
tiles to make  
the # in the radical

$$2 \frac{4}{5}$$

$$\sqrt{12}$$



$$3 \frac{3}{7}$$



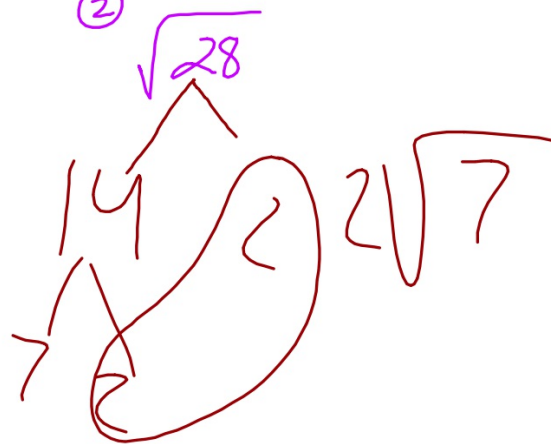
8/12 Do Now:

Factor to find the exact answer:

①



②



$$\begin{array}{c}
 \sqrt{192} \\
 \wedge \\
 (2) \quad 96 \\
 \wedge \\
 32 \quad 3 \\
 \wedge \\
 8 \quad 4 \\
 \wedge \\
 4 \quad 2 \quad (2) \\
 \wedge \\
 (2) \quad 2 \quad (2) \\
 \cdot 2 \cdot 2 \cdot 2 \cdot \sqrt{3} \\
 \boxed{8\sqrt{3}}
 \end{array}$$

$$\begin{array}{c}
 \sqrt{32} \\
 \wedge \\
 4 \quad 8 \\
 \wedge \quad \wedge \\
 (2) \quad 2 \quad 4 \quad 2 \\
 \wedge \quad \wedge \\
 (2) \quad 2 \\
 \cdot 2 \cdot 2 \cdot \sqrt{2} \\
 4\sqrt{2}
 \end{array}$$

$$\begin{array}{c}
 \sqrt{27} \\
 \wedge \\
 9 \quad 3 \\
 \wedge \\
 (3) \quad 3 \\
 3\sqrt{3}
 \end{array}$$

## Adding and Subtracting Radicals:

- you must have common radicals to get an exact answer

Ex:  $2\sqrt{5} + 3\sqrt{5}$  ;  $11\sqrt{6} - 2\sqrt{6}$  ;  $\sqrt{13} + 7\sqrt{13}$

$$2\sqrt{5} + 3\sqrt{5}$$

$$\boxed{5\sqrt{5}}$$

$$11\sqrt{6} - 2\sqrt{6}$$

$$\boxed{9\sqrt{6}}$$

$$\sqrt{13} + 7\sqrt{13}$$

$$\boxed{8\sqrt{13}}$$

• What happens when the radicals are not common?

① Simplify radicals to make them common.

② If your radicals can't be made common, leave it!

Ex:  $3\sqrt{8} + 12\sqrt{2}$

$\begin{array}{c} \wedge \\ 4 \cdot 2 \\ \wedge \\ (2 \cdot 2) \end{array}$

$3 \cdot 2\sqrt{2}$

$6\sqrt{2} + 12\sqrt{2}$

$18\sqrt{2}$

Ex:  $2\sqrt{15} + 3\sqrt{5}$

$\begin{array}{c} \wedge \\ 3 \cdot 5 \end{array}$

$2\sqrt{15} + 3\sqrt{5}$

$$\begin{aligned} \textcircled{1} \quad & 3\sqrt{18} - 2\sqrt{8} \\ & \begin{array}{c} \downarrow \quad \uparrow \\ 2 \quad 9 \\ \quad \uparrow \\ \textcircled{3 \quad 3} \end{array} \quad \begin{array}{c} \downarrow \quad \uparrow \\ 4 \quad 2 \\ \quad \uparrow \\ \textcircled{2 \quad 2} \end{array} \\ & 3 \cdot 3\sqrt{2} \quad 2 \cdot 2\sqrt{2} \\ & 9\sqrt{2} - 4\sqrt{2} \\ & \boxed{5\sqrt{2}} \end{aligned}$$

$$\textcircled{2} \quad \sqrt{5} + 5$$

$$\textcircled{\sqrt{5} + 5}$$

$$\textcircled{3} \quad 4\sqrt{24} + 8\sqrt{6}$$

$\begin{array}{c} \wedge \\ 4 \quad 6 \\ \wedge \quad \wedge \\ \underline{2 \quad 2} \quad \underline{3 \quad 2} \end{array}$

$4 \cdot 2\sqrt{6}$   
 $8\sqrt{6} + 8\sqrt{6}$

$16\sqrt{6}$

$$\textcircled{4} \quad \sqrt{52} + \sqrt{144}$$

$\begin{array}{c} \wedge \\ 26 \quad 2 \\ \wedge \\ \underline{13} \quad \underline{2} \end{array}$

$12$

$2\sqrt{13} + 12$

Steps to Multiplying Radicals:

- ① Multiply the #'s on the outside of the radical together.
- ② Multiply the # on the inside of the radical together.
- ③ Simplify.

$$4\sqrt{3}$$

Ex:  $(\sqrt{6})(\sqrt{8})$

$$\begin{array}{c} \sqrt{48} \\ \swarrow \quad \searrow \\ 6 \quad 8 \\ \swarrow \quad \searrow \quad \swarrow \quad \searrow \\ 3 \quad 2 \quad 4 \quad 2 \\ \hline \quad \quad \quad \triangle \\ \quad \quad \quad 2 \quad 2 \\ \hline 2 \cdot 2 \sqrt{3} \end{array}$$

Do Now:

$$3\sqrt{48} +$$

3  
24  
6 4  
3 2 2  
3 · 2 · 2√3  
12√3 +

$$5\sqrt{27}$$

9 3  
3 3  
5 · 3√3  
15√3

$$27\sqrt{3}$$



$$(\underline{3}\sqrt{\underline{5}})(\underline{11}\sqrt{\underline{13}})$$

$$33\sqrt{65}$$

13 5

$$33\sqrt{65}$$

$$320\sqrt{5}$$

$$(\underline{8}\sqrt{\underline{8}})(\underline{10}\sqrt{\underline{10}})$$

$$80\sqrt{80}$$

10 8

5 (2) 4 (2)

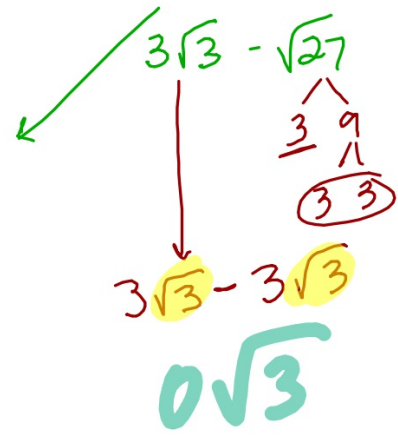
(2) (2)

$$80 \cdot 2 \cdot 2 \sqrt{5}$$

Addition / Subtraction

- |                  |                  |
|------------------|------------------|
| ① $-\sqrt{6}$    | ⑥ $-7\sqrt{17}$  |
| ② $\sqrt{7}$     | ⑦ $-21\sqrt{11}$ |
| ③ $-22\sqrt{21}$ | ⑧ $7\sqrt{3}$    |
| ④ $\sqrt{15}$    | ⑨ $-2\sqrt{6}$   |
| ⑤ $2\sqrt{7}$    | ⑩ $11\sqrt{6}$   |

- ⑪  $\sqrt{3}$   
⑫ 0



$$\textcircled{1} 3\sqrt{6} - 4\sqrt{6}$$

$$-\sqrt{6}$$

$$-\sqrt{6}$$





